

# Common fixed point theorems for mappings satisfying (E.A)-property via C-class functions in b-metric spaces

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## ABSTRACT

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*In this paper, we consider and generalize recent  $b$ -(E.A)-property results in [11] via the concepts of C-class functions in  $b$ -metric spaces. A example is given to support the result.*

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## 1. INTRODUCTION AND PRELIMINARIES

Bakhtin in [5] introduced the concept of  $b$ -metric space and prove the Banach fixed point theorem in the setting of  $b$ -metric spaces. Since then many authors have obtain various generalizations of fixed point theorems in  $b$ -metric spaces.

On the other hand, Aamri and Moutaawakil in [1] introduced the idea of (E.A)-property in metric spaces. Later on some authors employed this concept to obtain some new fixed point results. See ([6, 10]).

In this paper, we prove common fixed point results for two pairs of mappings which satisfy the  $b$  - (E.A)-property using the concept of C-class functions in  $b$ -metric spaces.

**Definition 1.1** ([5]). Let  $X$  be a nonempty set and  $s \geq 1$  be a given real number. A function  $d : X \times X \rightarrow [0, \infty)$  is a  $b$ -metric if, for all  $x, y, z \in X$ , the following conditions are satisfied:

- (b1)  $d(x, y) = 0$  if and only if  $x = y$ ,
- (b2)  $d(x, y) = d(y, x)$ ,
- (b3)  $d(x, z) \leq s[d(x, y) + d(y, z)]$ .

In this case, the pair  $(X, d)$  is called a  $b$ -metric space.

It should be noted that, the class of  $b$ -metric spaces is effectively larger than that of metric spaces, every metric is a  $b$ -metric with  $s = 1$ .

However, if  $(X, d)$  is a metric space, then  $(X, \rho)$  is not necessarily a metric space.

**Definition 1.2** ([7]). Let  $\{x_n\}$  be a sequence in a  $b$ -metric space  $(X, d)$ .

- (a)  $\{x_n\}$  is called  $b$ -convergent if and only if there is  $x \in X$  such that  $d(x_n, x) \rightarrow 0$  as  $n \rightarrow \infty$ .
- (b)  $\{x_n\}$  is a  $b$ -Cauchy sequence if and only if  $d(x_n, x_m) \rightarrow 0$  as  $n, m \rightarrow \infty$ .

A  $b$ -metric space is said to be complete if and only if each  $b$ -Cauchy sequence in this space is  $b$ -convergent.

**Proposition 1.3** ([7]). In a  $b$ -metric space  $(X, d)$ , the following assertions hold:

- (p1) A  $b$ -convergent sequence has a unique limit.
- (p2) Each  $b$ -convergent sequence is  $b$ -Cauchy.
- (p3) In general, a  $b$ -metric is not continuous.

**Definition 1.4** ([7]). Let  $(X, d)$  be a  $b$ -metric space. A subset  $Y \subset X$  is called closed if and only if for each sequence  $\{x_n\}$  in  $Y$  is  $b$ -convergent and converges to an element  $x$ .

**Definition 1.5** ([11]). Let  $(X, d)$  be a  $b$ -metric space and  $f$  and  $g$  be self-mappings on  $X$ .

- (i)  $f$  and  $g$  are said to compatible if whenever a sequence  $\{x_n\}$  in  $X$  is such that  $\{fx_n\}$  and  $\{gx_n\}$  are  $b$ -convergent to some  $t \in X$ , then

$$\lim_{n \rightarrow \infty} d(fgx_n, gfx_n) = 0.$$

- (ii)  $f$  and  $g$  are said to noncompatible if there exists at least one sequence  $\{x_n\}$  in  $X$  is such that  $\{fx_n\}$  and  $\{gx_n\}$  are  $b$ -convergent to some  $t \in X$ , but  $\lim_{n \rightarrow \infty} d(fgx_n, gfx_n)$  does not exist.

- (iii)  $f$  and  $g$  are said to satisfy the  $b - (E.A)$ -property if there exists a sequence  $\{x_n\}$  such that

$$\lim_{n \rightarrow \infty} fx_n = \lim_{n \rightarrow \infty} gx_n = t,$$

for some  $t \in X$ .

**Remark 1.6** ([11]). Noncompatibility implies property  $(E.A)$ .

**Example 1.7** ([11]).  $X = [0, 2]$  and define  $d : X \times X \rightarrow [0, \infty)$  as follows

$$d(x, y) = (x - y)^2.$$

Let  $f, g : X \rightarrow X$  be defined by

$$f(x) = \begin{cases} 1, & x \in [0, 1] \\ \frac{x+1}{8}, & x \in (1, 2] \end{cases} \quad g(x) = \begin{cases} \frac{3-x}{2}, & x \in [0, 1] \\ \frac{x}{4}, & x \in (1, 2] \end{cases}$$

For a sequence  $\{x_n\}$  in  $X$  such that  $x_n = 1 + \frac{1}{n+2}$ ,  $n = 0, 1, 2, \dots$ ,

$$\lim_{n \rightarrow \infty} fx_n = \lim_{n \rightarrow \infty} gx_n = \frac{1}{4}.$$

So  $f$  and  $g$  are satisfy the  $b - (E.A)$ -property. But

$$\lim_{n \rightarrow \infty} d(fgx_n, gfx_n) \neq 0.$$

Thus  $f$  and  $g$  are noncompatible.

**Definition 1.8** ([8]). Let  $f$  and  $g$  be given self-mappings on a set  $X$ . The pair  $(f, g)$  is said to be weakly compatible if  $f$  and  $g$  commute at their coincidence points (i.e.  $fgx = gfx$  whenever  $fx = gx$ ).

In 2014, Ansari [3] introduced the concept of  $C$ -class functions. See also [4]

**Definition 1.9.** A mapping  $F : [0, \infty)^2 \rightarrow \mathbb{R}$  is called  $C$ -class function if it is continuous and satisfies following axioms:

- (i)  $F(s, t) \leq s$ ;
- (ii)  $F(s, t) = s$  implies that either  $s = 0$  or  $t = 0$ ; for all  $s, t \in [0, \infty)$ .

Note for some  $F$  we have that  $F(0, 0) = 0$ .

We denote  $C$ -class functions as  $\mathcal{C}$ .

**Example 1.10.** The following functions  $F : [0, \infty)^2 \rightarrow \mathbb{R}$  are elements of  $\mathcal{C}$ , for all  $s, t \in [0, \infty)$ :

- (1)  $F(s, t) = s - t$ ,  $F(s, t) = s \Rightarrow t = 0$ ;
- (2)  $F(s, t) = ms$ ,  $0 < m < 1$ ,  $F(s, t) = s \Rightarrow s = 0$ ;
- (3)  $F(s, t) = \frac{s}{(1+t)^r}$ ;  $r \in (0, \infty)$ ,  $F(s, t) = s \Rightarrow s = 0$  or  $t = 0$ ;
- (4)  $F(s, t) = \log(t + a^s)/(1 + t)$ ,  $a > 1$ ,  $F(s, t) = s \Rightarrow s = 0$  or  $t = 0$ ;
- (5)  $F(s, t) = \ln(1 + a^s)/2$ ,  $a > e$ ,  $F(s, 1) = s \Rightarrow s = 0$ ;
- (6)  $F(s, t) = (s + l)^{(1/(1+t)^r)} - l$ ,  $l > 1$ ,  $r \in (0, \infty)$ ,  $F(s, t) = s \Rightarrow t = 0$ ;
- (7)  $F(s, t) = s \log_{t+a} a$ ,  $a > 1$ ,  $F(s, t) = s \Rightarrow s = 0$  or  $t = 0$ ;
- (8)  $F(s, t) = s - (\frac{1+s}{2+s})(\frac{t}{1+t})$ ,  $F(s, t) = s \Rightarrow t = 0$ ;
- (9)  $F(s, t) = s\beta(s)$ ,  $\beta : [0, \infty) \rightarrow (0, 1)$ , and is continuous,  $F(s, t) = s \Rightarrow s = 0$ ;
- (10)  $F(s, t) = s - \frac{t}{k+t}$ ,  $F(s, t) = s \Rightarrow t = 0$ ;
- (11)  $F(s, t) = s - \varphi(s)$ ,  $F(s, t) = s \Rightarrow s = 0$ , here  $\varphi : [0, \infty) \rightarrow [0, \infty)$  is a continuous function such that  $\varphi(t) = 0 \Leftrightarrow t = 0$ ;
- (12)  $F(s, t) = sh(s, t)$ ,  $F(s, t) = s \Rightarrow s = 0$ , here  $h : [0, \infty) \times [0, \infty) \rightarrow [0, \infty)$  is a continuous function such that  $h(t, s) < 1$  for all  $t, s > 0$ ;
- (13)  $F(s, t) = s - (\frac{2+t}{1+t})t$ ,  $F(s, t) = s \Rightarrow t = 0$ .

- (14)  $F(s, t) = \sqrt[n]{\ln(1 + s^n)}$ ,  $F(s, t) = s \Rightarrow s = 0$ .  
 (15)  $F(s, t) = \phi(s)$ ,  $F(s, t) = s \Rightarrow s = 0$ , here  $\phi : [0, \infty) \rightarrow [0, \infty)$  is an upper semicontinuous function such that  $\phi(0) = 0$ , and  $\phi(t) < t$  for  $t > 0$ ,  
 (16)  $F(s, t) = \frac{s}{(1+s)^r}$ ;  $r \in (0, \infty)$ ,  $F(s, t) = s \Rightarrow s = 0$ .

**Definition 1.11** ([9]). A function  $\psi : [0, \infty) \rightarrow [0, \infty)$  is called an altering distance function if the following properties are satisfied:

- (i)  $\psi$  is non-decreasing and continuous,
- (ii)  $\psi(t) = 0$  if and only if  $t = 0$ .

See also [2] and [12].

**Definition 1.12** ([3]). An ultra altering distance function is a continuous, nondecreasing mapping  $\varphi : [0, \infty) \rightarrow [0, \infty)$  such that  $\varphi(t) > 0$ ,  $t > 0$  and  $\varphi(0) \geq 0$ .

## 2. MAIN RESULTS

Through out this section, we assume  $\psi$  is altering distance function,  $\varphi$  is ultra altering distance function and  $F$  is a C-class function. We shall start the following theorem.

**Theorem 2.1.** Let  $(X, d)$  be a  $b$ -metric space and  $f, g, S, T : X \rightarrow X$  be mappings with  $f(X) \subseteq T(X)$  and  $g(X) \subseteq S(X)$  such that

$$(2.1) \quad \psi(d(fx, gy)) \leq F(\psi(M_s(x, y)), \varphi(M_s(x, y))), \quad \text{for all } x, y \in X$$

where,

$$M_s(x, y) = \max \left\{ d(Sx, Ty), d(fx, Sx), d(gy, Ty), \frac{d(fx, Ty) + d(Sx, gy)}{2s} \right\}.$$

Suppose that one of the pairs  $(f, S)$  and  $(g, T)$  satisfy the  $b - (E.A)$ -property and that one of the subspaces  $f(X)$ ,  $g(X)$ ,  $S(X)$  and  $T(X)$  is closed in  $X$ . Then the pairs  $(f, S)$  and  $(g, T)$  have a point of coincidence in  $X$ . Moreover, if the pairs  $(f, S)$  and  $(g, T)$  are weakly compatible, then  $f, g, S$  and  $T$  have a unique common fixed point.

*Proof.* If the pairs  $(f, S)$  satisfies the  $b - (E.A)$ -property, then there exists a sequence  $\{x_n\}$  in  $X$  satisfying

$$\lim_{n \rightarrow \infty} fx_n = \lim_{n \rightarrow \infty} Sx_n = q,$$

for some  $q \in X$ . As  $f(X) \subseteq T(X)$  there exists a sequence  $\{y_n\}$  in  $X$  such that  $fx_n = Ty_n$ . Hence  $\lim_{n \rightarrow \infty} Ty_n = q$ . Let us show that  $\lim_{n \rightarrow \infty} gy_n = q$ . By (2.1),

$$(2.2) \quad \psi(d(fx_n, gy_n)) \leq F(\psi(M_s(x_n, y_n)), \varphi(M_s(x_n, y_n))) \leq \psi(M_s(x_n, y_n))$$

where

$$\begin{aligned} M_s(x_n, y_n) &= \max \left\{ d(Sx_n, Ty_n), d(fx_n, Sx_n), d(Ty_n, gy_n), \frac{d(Sx_n, gy_n) + d(fx_n, Ty_n)}{2s} \right\} \\ &= \max \left\{ d(Sx_n, fx_n), d(fx_n, gy_n), \frac{d(Sx_n, gy_n) + d(fx_n, fx_n)}{2s} \right\} \\ &\leq \max \left\{ d(Sx_n, fx_n), d(fx_n, gy_n), \frac{s[d(Sx_n, fx_n), d(fx_n, gy_n)]}{2s} \right\}. \end{aligned}$$

In (2.2), on taking limit,

$$\psi(\lim_{n \rightarrow \infty} d(q, gy_n)) \leq F(\psi(\lim_{n \rightarrow \infty} d(q, gy_n)), \varphi(\lim_{n \rightarrow \infty} d(q, gy_n))).$$

So,  $\psi(\lim_{n \rightarrow \infty} d(q, gy_n)) = 0$ , or  $\varphi(\lim_{n \rightarrow \infty} d(q, gy_n)) = 0$ . Thus

$$\lim_{n \rightarrow \infty} d(q, gy_n) = 0.$$

Hence  $\lim_{n \rightarrow \infty} gy_n = q$ .

If  $T(X)$  is closed subspace of  $X$ , then there exists a  $r \in X$ , such that  $Tr = q$ . By (2.1),

$$(2.3) \quad \psi(d(fx_n, gr)) \leq F(\psi(M_s(x_n, r)), \varphi(M_s(x_n, r)))$$

where

$$\begin{aligned} M_s(x_n, r) &= \max \left\{ d(Sx_n, Tr), d(fx_n, Sx_n), d(Tr, gr), \frac{d(fx_n, Tr) + d(Sx_n, gr)}{2s} \right\} \\ &= \max \left\{ d(Sx_n, q), d(fx_n, Sx_n), d(q, gr), \frac{d(fx_n, q) + d(Sx_n, gr)}{2s} \right\}. \end{aligned}$$

Letting  $n \rightarrow \infty$ ,

$$\begin{aligned} \lim_{n \rightarrow \infty} M_s(x_n, r) &= \max \left\{ d(q, q), d(q, q), d(q, gr), \frac{d(q, q) + d(q, gr)}{2s} \right\} \\ &= d(q, gr). \end{aligned}$$

Now, (2.3) and definition of  $\psi$  and  $\varphi$ , as  $n \rightarrow \infty$ ,

$$\psi(d(q, gr)) \leq F(\psi(d(q, gr)), \varphi(d(q, gr)))$$

which implies  $\psi(d(q, gr)) = 0$  or  $\varphi(d(q, gr)) = 0$  gives  $gr = q$ . Thus  $r$  is a coincidence point of the pair  $(g, T)$ . As  $g(X) \subseteq S(X)$ , there exists a point  $z \in X$  such that  $q = Sz$ . We claim that  $Sz = fz$ . By (2.1), we have

$$(2.4) \quad \psi(d(fz, gr)) \leq F(\psi(M_s(z, r)), \varphi(M_s(z, r)))$$

where

$$\begin{aligned}
 M_s(z, r) &= \max \left\{ d(Sz, Tr), d(fz, Sz), d(Tr, gr), \frac{d(fz, Tr) + d(Sz, gr)}{2s} \right\} \\
 &= \max \left\{ d(q, q), d(fz, q), d(q, q), \frac{d(fz, q) + d(q, q)}{2s} \right\} \\
 &\leq \max \left\{ d(fz, q), \frac{d(fz, q)}{2s} \right\} \\
 &= d(fz, q).
 \end{aligned}$$

Thus from (2.4),

$$\psi(d(fz, gr)) = \psi(d(fz, q)) \leq F(\psi(d(fz, q)), \varphi(d(fz, q)))$$

implies that  $\psi(d(fz, q)) = 0$ , or  $\varphi(d(fz, q)) = 0$ . Therefore  $Sz = fz = q$ . Hence  $z$  is a coincidence point of the pair  $(f, S)$ . Thus  $fz = Sz = gr = Tr = q$ . By weak compatibility of the pairs  $(f, S)$  and  $(g, T)$ , we deduce that  $fz = Sq$  and  $gq = Tq$ . We will show that  $q$  is a common fixed point of  $f, g, S$  and  $T$ . From (2.1),

$$(2.5) \quad \psi(d(fq, q)) = \psi(d(fq, gr)) \leq F(\psi(M_s(q, r)), \varphi(M_s(q, r)))$$

where,

$$\begin{aligned}
 M_s(q, r) &= \max \left\{ d(Sq, Tr), d(fq, Sq), d(Tr, gr), \frac{d(fq, Tr) + d(Sq, gr)}{2s} \right\} \\
 &= \max \left\{ d(fq, q), d(fq, fq), d(q, q), \frac{d(fq, q) + d(fq, q)}{2s} \right\} \\
 &= d(fq, q).
 \end{aligned}$$

By (2.5)

$$\psi(d(fq, q)) \leq F(\psi(d(fq, q)), \varphi(d(fq, q))).$$

So  $fq = Sq = q$ . Similarly, it can be shown  $gq = Tq = q$ .

To prove the uniqueness of the fixed point of  $f, g, S$  and  $T$ . Suppose for contradiction that  $p$  is another fixed point of  $f, g, S$  and  $T$ . By (2.1), we obtain

$$\psi(d(q, p)) = \psi(d(fq, gp)) \leq F(\psi(M_s(q, p)), \varphi(M_s(q, p)))$$

and

$$\begin{aligned}
 M_s(q, p) &= \max \left\{ d(Sq, Tp), d(fq, Sq), d(Tp, gp), \frac{d(fq, Tp) + d(Sq, gp)}{2s} \right\} \\
 &= \max \left\{ d(q, p), d(q, q), d(p, p), \frac{d(q, p) + d(q, p)}{2s} \right\} \\
 &= d(q, p).
 \end{aligned}$$

Hence we have

$$\psi(d(q, p)) \leq F(\psi(d(q, p)), \varphi(d(q, p))),$$

which implies that  $\psi(d(q, p)) = 0$  or  $\varphi(d(q, p)) = 0$ . So  $q = p$ .  $\square$

**Corollary 2.2.** Let  $(X, d)$  be a  $b$ -metric space and  $f, g, S, T : X \rightarrow X$  be mappings with  $f(X) \subseteq T(X)$  and  $g(X) \subseteq S(X)$  such that

$$d(fx, gy) \leq F(M_s(x, y), \varphi(M_s(x, y))), \text{ for all } x, y \in X,$$

where

$$M_s(x, y) = \max \left\{ d(Sx, Ty), d(fx, Sx), d(gy, Ty), \frac{d(fx, Ty) + d(Sx, gy)}{2s} \right\}.$$

Suppose that one of the pairs  $(f, S)$  and  $(g, T)$  satisfy the  $b$ -(E.A)-property and that one of the subspaces  $f(X), g(X), S(X)$  and  $T(X)$  is closed in  $X$ . Then the pairs  $(f, S)$  and  $(g, T)$  have a point of coincidence in  $X$ . Moreover, if the pairs  $(f, S)$  and  $(g, T)$  are weakly compatible, then  $f, g, S$  and  $T$  have a unique common fixed point.

**Corollary 2.3.** Let  $(X, d)$  be a  $b$ -metric space and  $f, T : X \rightarrow X$  be mappings such that

$$\psi(d(fx, fy)) \leq F(\psi(M_s(x, y)), \varphi(M_s(x, y))), \text{ for all } x, y \in X,$$

where

$$M_s(x, y) = \max \left\{ d(Tx, Ty), d(fx, Tx), d(fy, Ty), \frac{d(fx, Ty) + d(Tx, fy)}{2s} \right\}.$$

Suppose that the pair  $(f, T)$  satisfies the  $b$ -(E.A)-property and  $T(X)$  is closed in  $X$ . Then the pair  $(f, T)$  has a common point of coincidence in  $X$ . Moreover, if the pair  $(f, T)$  is weakly compatible, then  $f$  and  $T$  have a unique common fixed point.

**Example 2.4.** Let  $F(s, t) = \frac{99}{100}s$ ,  $X = [0, 1]$  and define  $d : X \times X \rightarrow [0, \infty)$  as follows

$$d(x, y) = \begin{cases} 0, & x = y \\ (x + y)^2, & x \neq y \end{cases}$$

Then  $(X, d)$  is a  $b$ -metric space with constant  $s = 2$ . Let  $f, g, S, T : X \rightarrow X$  be defined by

$$\begin{aligned} f(x) &= \frac{x}{4}, \quad g(x) = \begin{cases} 0, & x \neq \frac{1}{2} \\ \frac{1}{8}, & x = \frac{1}{2} \end{cases}, \quad S(x) = \begin{cases} 2x, & 0 \leq x < \frac{1}{2} \\ \frac{1}{8}, & \frac{1}{2} \leq x \leq 1 \end{cases} \text{ and} \\ T(x) &= \begin{cases} x, & 0 \leq x < \frac{1}{2} \\ \frac{1}{2}, & \frac{1}{2} \leq x \leq 1 \end{cases}. \end{aligned}$$

Clearly,  $f(X)$  is closed and  $f(X) \subseteq T(X)$  and  $g(X) \subseteq S(X)$ . The sequence  $\{x_n\}$ ,  $x_n = \frac{1}{2} + \frac{1}{n}$ , is in  $X$  such that  $\lim_{n \rightarrow \infty} fx_n = \lim_{n \rightarrow \infty} Sx_n = \frac{1}{8}$ . So that the pair  $(f, S)$  satisfies the  $b$ -(E.A)-property. But the pair  $(f, S)$  is noncompatible for  $\lim_{n \rightarrow \infty} d(fSx_n, Sfx_n) \neq 0$ . The altering functions  $\psi, \varphi : [0, \infty) \rightarrow [0, \infty)$  are defined by  $\psi(t) = \sqrt{t}$ . To check the contractive condition (2.1), for all  $x, y \in X$ ,

if  $x = 0$  or  $x = \frac{1}{2}$ , then (2.1) is satisfied.

if  $x \in (0, \frac{1}{2})$ , then

$$\psi(d(fx, gy)) = \frac{x}{4} \leq \frac{99}{100} \frac{9x}{4} = \frac{99}{100} d(fx, Sx) \leq \frac{99}{100} \psi(M_s(x, y)).$$

If  $x \in (\frac{1}{2}, 1]$ , then

$$\psi(d(fx, gy)) = \frac{x}{4} \leq \frac{99}{100} \left( \frac{x}{4} + \frac{1}{8} \right) = \frac{99}{100} d(fx, Sx) \leq \frac{99}{100} \psi(M_s(x, y)).$$

Then (2.1) is satisfied for all  $x, y \in X$ . The pairs  $(f, S)$  and  $(g, T)$  are weakly compatible. Hence, all of the conditions of Theorem 2.1 are satisfied. Moreover 0 is the unique common fixed point of  $f, g, S$  and  $T$ .

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